

9. Is there an enumeration of  $\mathbb{Q}$  as  $q_1, q_2, q_3, \dots$  such that  $\sum(q_n - q_{n+1})^2$  is finite?
10. Write down a differentiable function  $f$  from  $[0, 1]$  to  $\mathbb{R}$  such that  $f'$  is not (Riemann) integrable. If  $f'$  is bounded, must it be integrable?
11. Find a continuous surjection from  $\mathbb{R}$  to  $\mathbb{R}^2$ .
12. Is there a continuous bijection from  $\mathbb{R}$  to  $\mathbb{R}^2$ ?
13. Construct a function from  $\mathbb{R}$  to  $\mathbb{R}$  that is infinitely-differentiable, but is identically 1 on  $[-1, 1]$  and identically 0 outside  $(-2, 2)$ .
14. A subset of  $\mathbb{R}$  is called *perfect* if it is closed and has no isolated points. Write down a (non-empty) perfect set that does not contain any (non-trivial) interval. Prove that every closed set is the union of a perfect set and a countable set.
15. Can a simple closed curve in the plane have positive area?